Mathematics: MCM 109 Final Exam: 12 - 6 - 2011Duration Time: 1 Hour **Answer 3 Questions Only**



Academic Year: 2010 – 2011

Semester: Spring

Examiner: Dr. Mohamed Eid

Marks

3

4

4

4

6

[1](a) Find y` where: (i) $y = 2x^3 + 8^x$

(ii)
$$y = \sin x + \log x$$
 (iii) $y = x^2 \tan x$

 $(ii)\int [x+\frac{1}{x}]^2 dx$

(b) Find the integrals: (i)
$$\int (2x^3 - 3^x) dx$$
 (ii) $\int [x + \frac{1}{x}] dx$ (c) Find the eigenvalues and eigenvectors of the matrix $A = \begin{bmatrix} -2 & 4 \\ 0 & 3 \end{bmatrix}$ 5

[2](a)Determine maximum and minimum values of :
$$f(x) = x^3 - 3x^2 - 9x$$

(b) Find the integrals: (i) $\int x \cdot 2^x dx$ (ii) $\int (x - \tan x) dx$

(c) If
$$A = \begin{bmatrix} 1 & 2 \\ -1 & 1 \\ 3 & 0 \end{bmatrix}$$
, $B = \begin{bmatrix} 1 & 2 \\ 3 & 6 \end{bmatrix}$. Find, if possible, $A + B$, $|A|$, $|B|$, $A \cdot B$, $B \cdot A = \begin{bmatrix} 1 & 2 \\ 3 & 6 \end{bmatrix}$.

[3](a) Find the inflection points of the function: $f(x) = x^3 - 9x + 2$

(b)If
$$A = \begin{bmatrix} 2 & 1 & 0 \\ 0 & 3 & -1 \end{bmatrix}$$
, $B = \begin{bmatrix} 1 & 3 & 2 \\ 1 & 0 & -2 \end{bmatrix}$. Find, if possible, $A + B$, $A \cdot B$, $A \cdot B$ 4

(c)Discuss the consistence of the following linear system (it has one solution, no solution or infinite solutions):

$$x + y + z = 3$$
, $x - y + 2z = 2$, $2x + y - 2z = 1$

[4](a)Find the integrals: (i)
$$\int_{1}^{2} (x^2 + \frac{1}{x^2}) dx$$
 (ii) $\int_{1}^{2} \frac{x+1}{x^2 - 5x + 6} dx$

(b) If a medicine is available in 3 dosage forms:

First type of concentration: 1 mg /tablet Second type of concentration: 2 mg/tablet

3 mg/tablet Third type of concentration:

If the pharmacist wanted to prepare 10 tablets containing 1.5 mg/tablet

by mixing whole tablets of each type. Find all possible solutions.

Good luck

Dr. Mohamed Eid

Academic Year: 2010 – 2011

Semester: Spring 4 - 5 - 2011Date:

Time: 60 Minutes Faculty of Pharmacy Mathematics: MCM 109

Mid-Term Exam

Examiner: Dr. Mohamed Eid

Answer all questions

[1] Find y` where: (a)
$$y = 2x^3 + 2^x$$

(c)
$$y = 8 + \log(x^3 + x)$$

(b)
$$y = \sin x \cdot \log x$$

(d) $y = x^{-3} + 3x$

[2] Find the integrals: (a)
$$\int (3^x + \cos x) dx$$

(b)
$$\int (3 + \frac{2x+1}{x^2 + x + 2}) dx$$

(c)
$$\int (\frac{1}{x^2} + \frac{1}{x} + x^2) dx$$

[3] Find the maximum and minimum values of the function: $f(x) = x^3 - 12x + 3$

[4] A drug in the blood decreases according to equation $\sqrt{y_0} - \sqrt{y} = 8t$.

If the initial quantity $y_0 = 200$ units. Find

(i) The time at which 30 % of drug exists in the blood.

(ii) The time at which 50 % of drug exists in the blood.

(iii) The time at which there is no drug in the blood.

Good luck

Dr. Mohamed Eid

- [1] If $A = \begin{bmatrix} 1 & 2 \\ 3 & 1 \\ 1 & 0 \end{bmatrix}$, $B = \begin{bmatrix} 2 & 1 & 3 \\ 1 & 0 & 2 \end{bmatrix}$. Find, if possible, $A^t + B$, A + B, A + B
- [2] Write the following linear system and discuss its consistence (it has one solution or no solution or infinite solutions): x + y + z = 6, x y + 2z = 2, 2x + 2y + 2z = 6
- [3] Find the eigenvalues and eigenvectors of the matrix $A = \begin{bmatrix} 3 & 1 \\ 4 & 0 \end{bmatrix}$

Good luck

Dr. Mohamed Eid